

About the radius of convexity of some analytic functions

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ABSTRACT.

In this paper we prove a general result regarding the radius of convexity for different particular functions. The method of convolutions is used. The results are applied to deduce sharp bounds regarding functions, which satisfy differential subordinations.

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