

A modified Seidel method for calculating the fixed points of contractive mappings

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ABSTRACT.

For calculating the fixed point of a contractive mapping $\mathbf{f} = (f_1, f_2, \dots, f_m) : \Omega \rightarrow \Omega$, $\Omega \in \mathbf{R}^m$ we employ a modified Seidel successive approximations scheme:

$$x_{\pi(k)}^{(n)} = f_{\pi(k)} \left(\tilde{x}_1^{(n,k)}, \dots, \tilde{x}_{k-1}^{(n,k)}, \tilde{x}_k^{(n,k)}, \dots, \tilde{x}_m^{(n,k)} \right),$$

where

$$\tilde{x}_l^{(n,k)} = \begin{cases} x_l^{(n)}, & \text{if } l = \pi(s) \text{ and } s < k, \\ x_l^{(n-1)}, & \text{if } l = \pi(s) \text{ and } s \geq k. \end{cases}$$

We present a strategy to find the permutation π in order to accelerate the iterative processus.

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